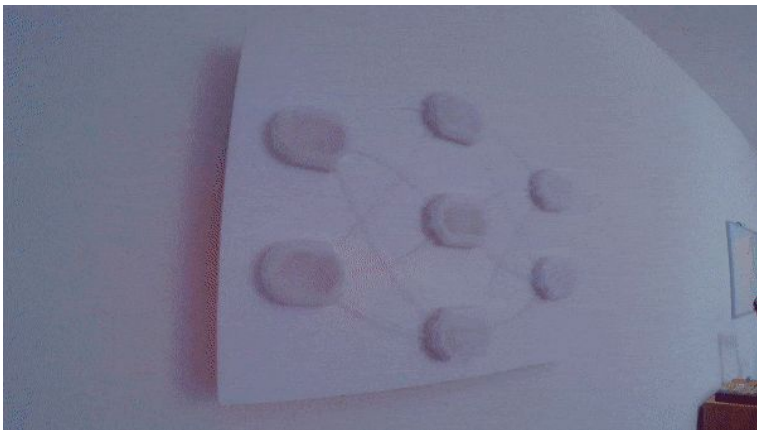


Shooting hoops with machine learning 🏀



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# Hola

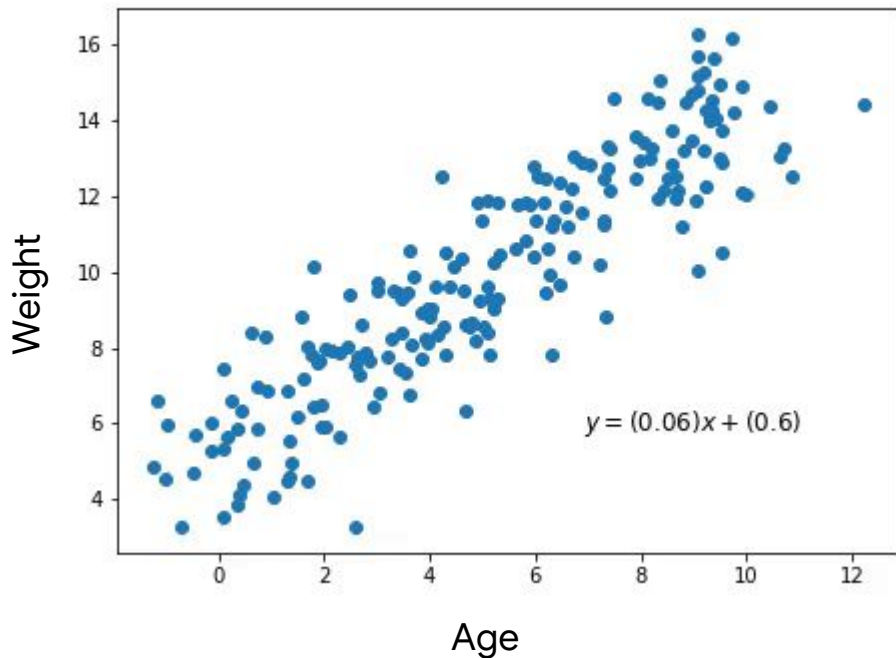


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## Linear Regression

*(the line of best fit)*



$$y = mx + c$$

$$\text{Weight} = (0.82) \text{Age} + 5.8$$

[bit.ly/zack-akil-line](https://bit.ly/zack-akil-line)

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*If I can't be **good** at it,*

*Can I look **cool** doing it? ☐*

















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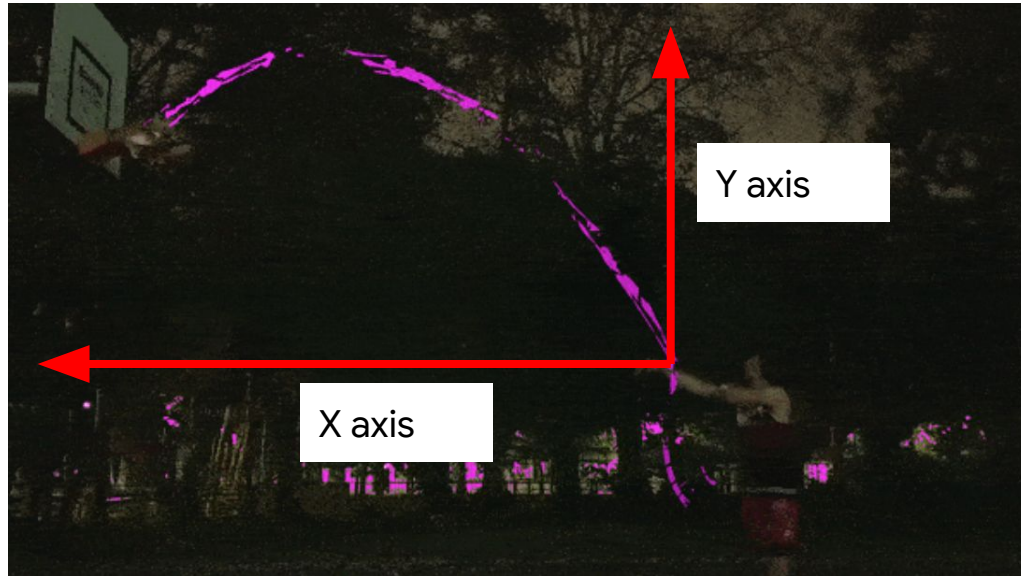
```
if (pixel_colour == white)
```



[bit.ly/zack-akil-ghost](https://bit.ly/zack-akil-ghost)

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Looks like data



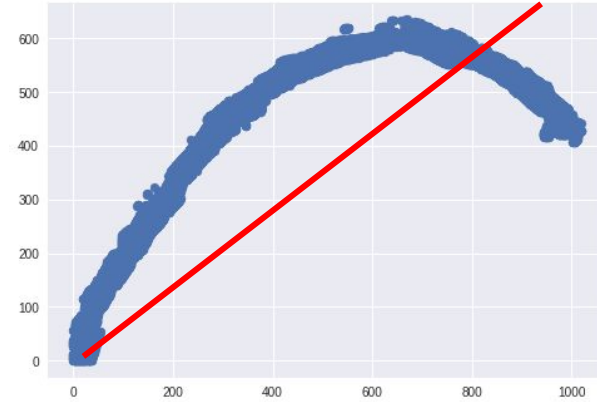


*If I can't be **good** at it,*

*Or look **cool** doing it,*

*Can I do some **Machine Learning**? ☐*

## Standard Linear Regression ( $y=mx+c$ ) 🙅







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## Trajectory

From Wikipedia, the free encyclopedia

*For other uses, see [Trajectory \(disambiguation\)](#).  
"Flightpath" redirects here. For other uses, see [Flightpath \(disambiguation\)](#).*

A **trajectory** or **flight path** is the path that a **object** with **mass** in **motion** follows through **space** as a function of time. In **classical mechanics**, a trajectory is defined by **Hamiltonian mechanics** via **canonical coordinates**; hence, a complete trajectory is defined by position and momentum, simultaneously. Trajectory in **quantum mechanics** is not defined due to Heisenberg **uncertainty principle** that position and momentum can not be measured simultaneously.

In classical mechanics, the mass might be a **projectile** or a **satellite**.<sup>[1]</sup> For example, it can be an **orbit**—the path of a **planet**, an **asteroid**, or a **comet** as it travels around a central mass.

In **control theory** a trajectory is a time-ordered set of **states** of a dynamical system (see e.g. **Poincaré map**). In **discrete mathematics**, a trajectory is a sequence  $(f^k(x))_{k \in \mathbb{N}}$  of values calculated by the iterated application of a mapping *f* to an element *x* of its source.

### Physics of trajectories [ edit ]

The motion of the particle is described by the second-order differential equation

$$m \frac{d^2 \vec{x}(t)}{dt^2} = -\nabla V(\vec{x}(t)) \text{ with } \vec{x} = (x, y, z).$$

### Examples [ edit ]

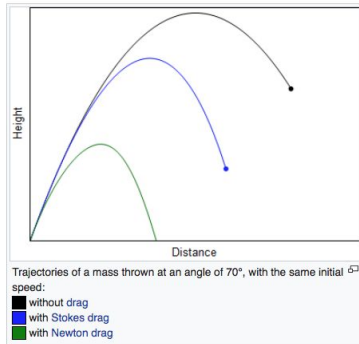
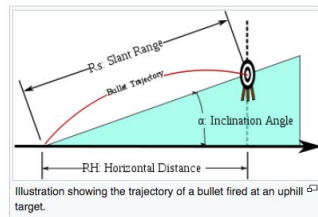
#### Uniform gravity, neither drag nor wind [ edit ]

The ideal case of motion of a projectile in a uniform gravitational field in the absence of other forces (such as air drag) was first investigated by Galileo Galilei. To neglect the action of the atmosphere in shaping a trajectory would have been considered a futile hypothesis by practical-minded investigators all through the **Middle Ages** in Europe. Nevertheless, by anticipating the existence of the **vacuum**, later to be demonstrated on Earth by his collaborator **Evangelista Torricelli**<sup>[*citation needed*]</sup>, Galileo was able to initiate the future science of **mechanics**.<sup>[*citation needed*]</sup> In a near vacuum, as it turns out for instance on the **Moon**, his simplified parabolic trajectory proves essentially correct.

In the analysis that follows, we derive the equation of motion of a projectile as measured from an inertial frame at rest with respect to the ground. Associated with the frame is a right-hand coordinate system with its origin at the point of launch of the projectile. The *x*-axis is tangent to the ground, and the *y*-axis is perpendicular to it ( parallel to the gravitational field lines ). Let *g* be the **acceleration of gravity**. Relative to the flat terrain, let the initial horizontal speed be *v<sub>h</sub>* = *v* cos(*θ*) and the initial vertical speed be *v<sub>v</sub>* = *v* sin(*θ*). It will also be shown that the **range** is 2*v<sub>h</sub>**v<sub>v</sub>*/*g*, and the maximum altitude is *v<sub>v</sub>*<sup>2</sup>/2*g*. The maximum range for a given initial speed *v* is obtained when *v<sub>h</sub>* = *v<sub>v</sub>*, i.e. the initial angle is 45°. This range is *v*<sup>2</sup>/*g*, and the maximum altitude at the maximum range is *v*<sup>2</sup>/(4*g*).

#### Derivation of the equation of motion [ edit ]

Assume the motion of the projectile is being measured from a **free fall** frame which happens to be at (*x*,*y*) = (0,0) at *t* = 0. The equation of motion of the projectile in this frame (by the **equivalence**



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$$y = \tan(\theta) \cdot x - \frac{gx^2}{2v^2\cos^2(\theta)}$$

[bit.ly/zack-akil-traj](https://bit.ly/zack-akil-traj)



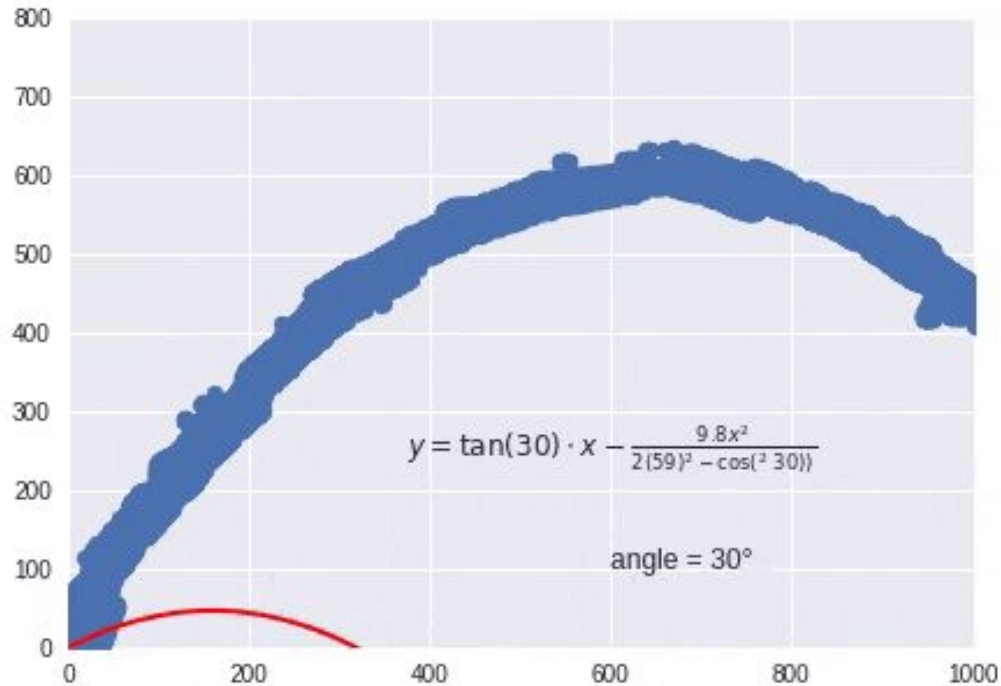
# TensorFlow

[bit.ly/zack-akil-traj-tf](https://bit.ly/zack-akil-traj-tf)

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# Fit equation to my shot



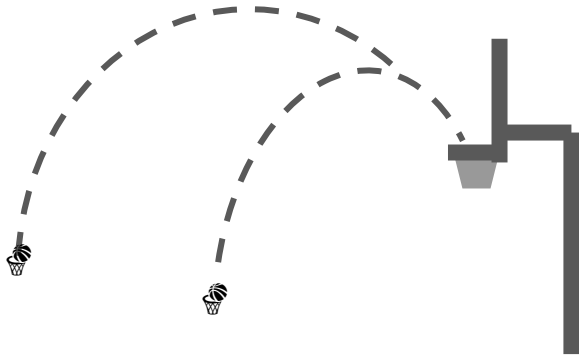
[bit.ly/zack-akil-traj-gif](https://bit.ly/zack-akil-traj-gif)

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# Consistency is key



*“Your technique shouldn’t change,  
the only thing that changes is the power”*

**- Anita Hoops-McGee**



# Shot analyse in 6 steps



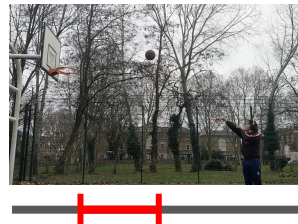
Record shot

🕒 10 minutes



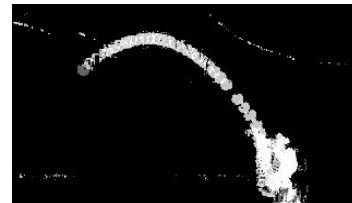
Go home

🕒 5 minutes (manual)



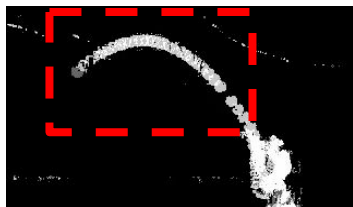
Trim video

🕒 < 1 second (automatic)



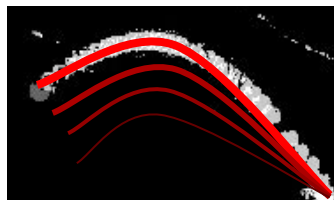
Apply pre-processing

🕒 5 minutes (manual)



Crop shot

🕒 1 second (automatic)



Run model

Your shot angle was 62°

# Shot analyse in 6 steps



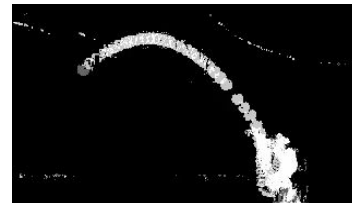
Record shot



Neural Network

Trim video


 < 1second (automatic)

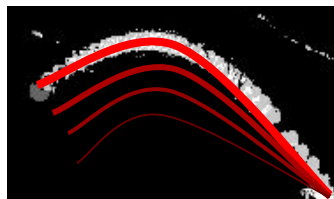


Apply pre-processing

Neural Network

Crop shot

 1second (automatic)

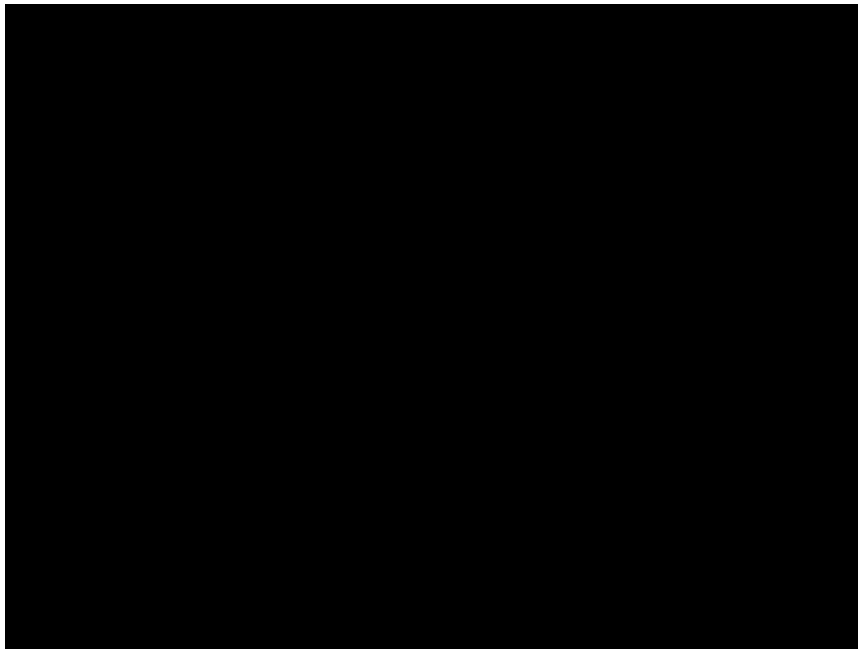


Run model

Your shot angle was 62°

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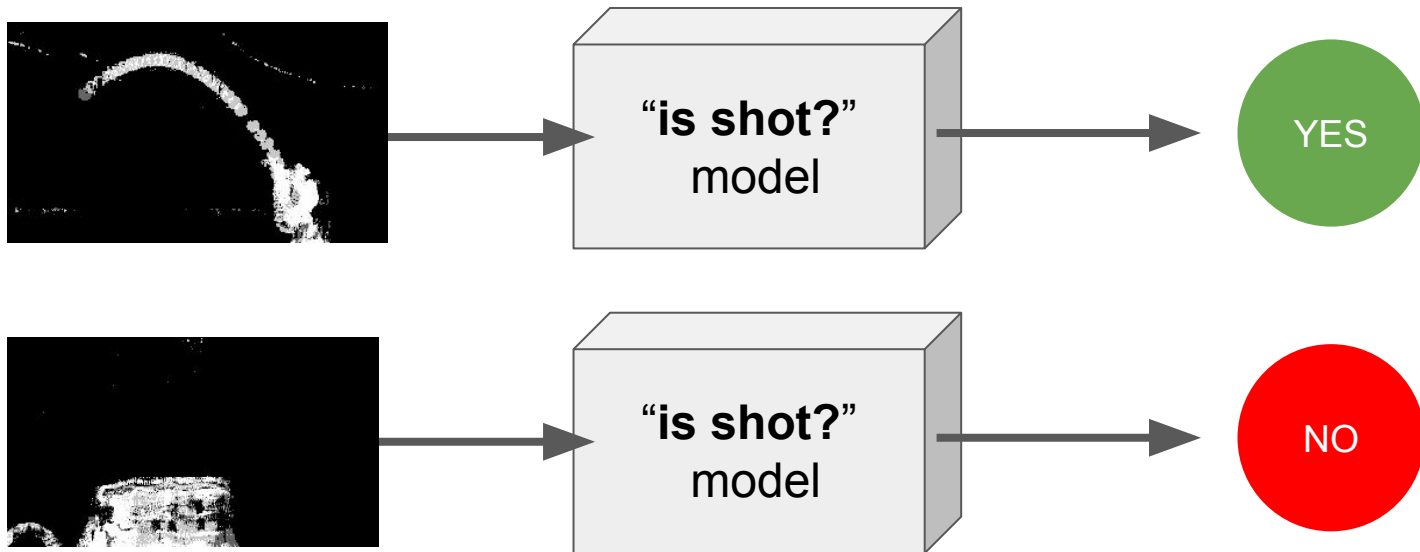
# Auto trimming model





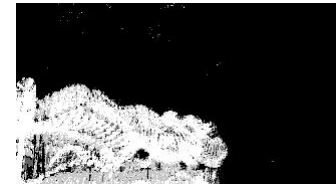
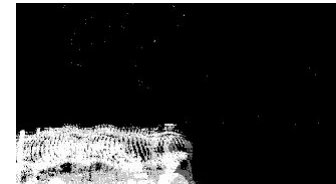
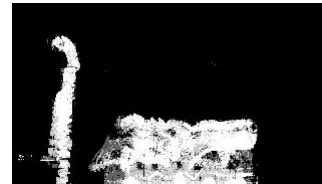
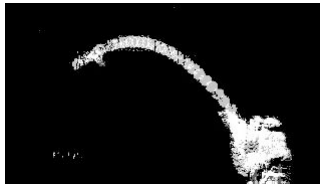
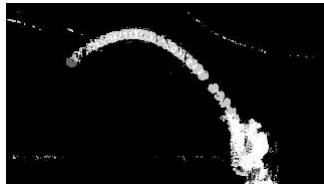
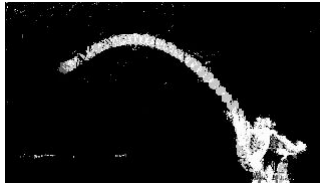
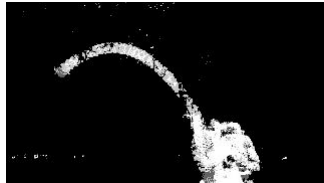
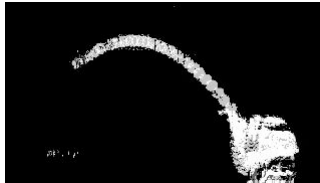
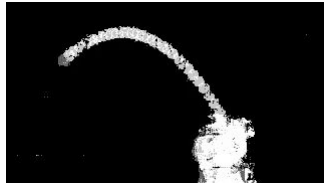
# Auto-trimming model

**Binary Classification Model**  
(“yes” or “no” model)



TRUE (yes)

FALSE (no)



# “is shot?” model



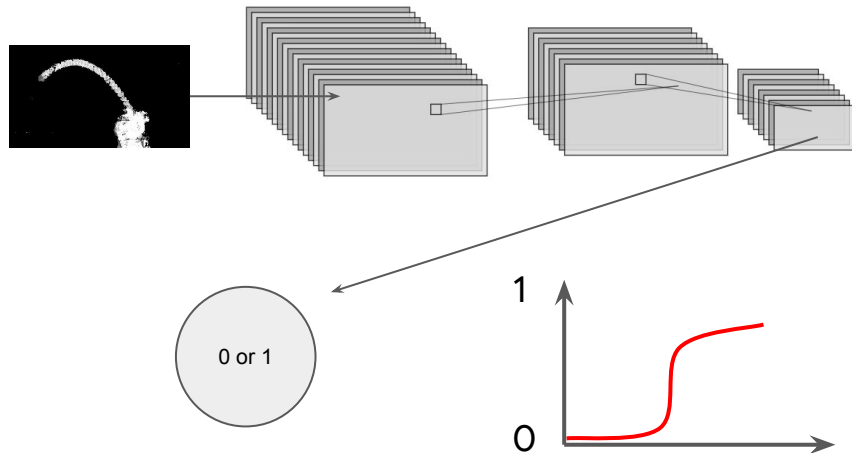
```
model = Sequential()

model.add(Conv2D(4, kernel_size=(3, 3),
                 activation='relu',
                 input_shape=input_shape))

model.add(MaxPooling2D(pool_size=(2, 2)))
model.add(Dropout(0.5))
model.add(Flatten())
model.add(Dense(8, activation='relu'))
model.add(Dropout(0.5))
model.add(Dense(1, activation='sigmoid'))
```

## Convolutional Neural Network (CNN)

*(Good at image based tasks)*







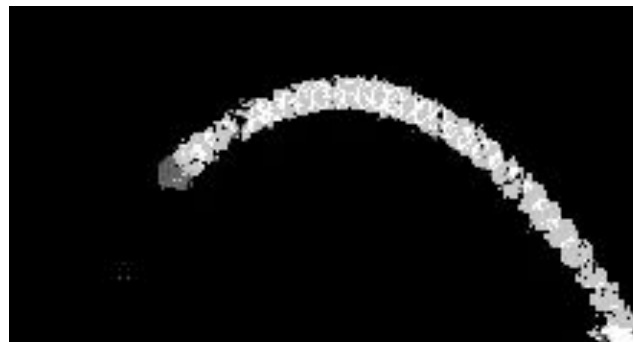
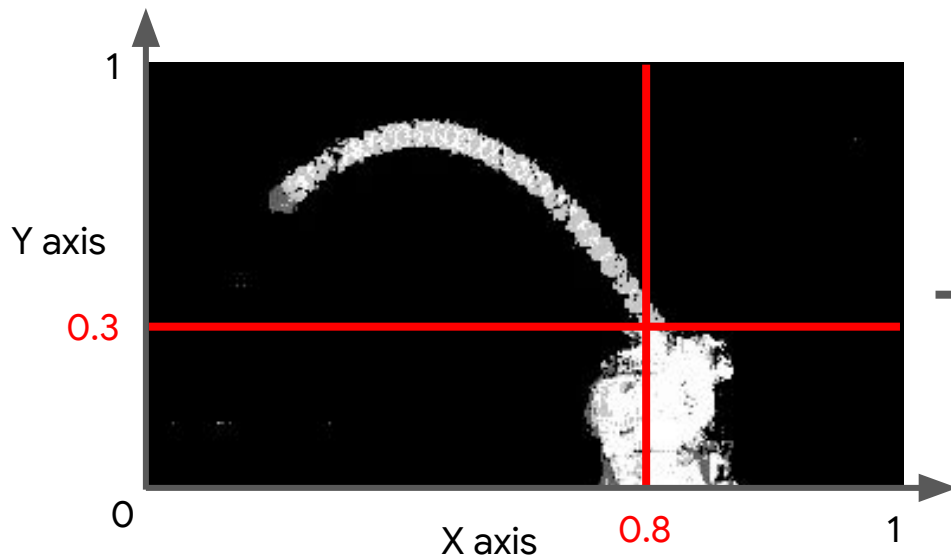
An outdoor basketball court with a black fence and asphalt surface. In the background, there are many trees with green and yellowing leaves, suggesting autumn. A basketball hoop is visible on the left, and another one is on the right. A semi-transparent grey box is centered over the image.

# Shot demo

[bit.ly/zack-akil-hoops-shot-demo](https://bit.ly/zack-akil-hoops-shot-demo)



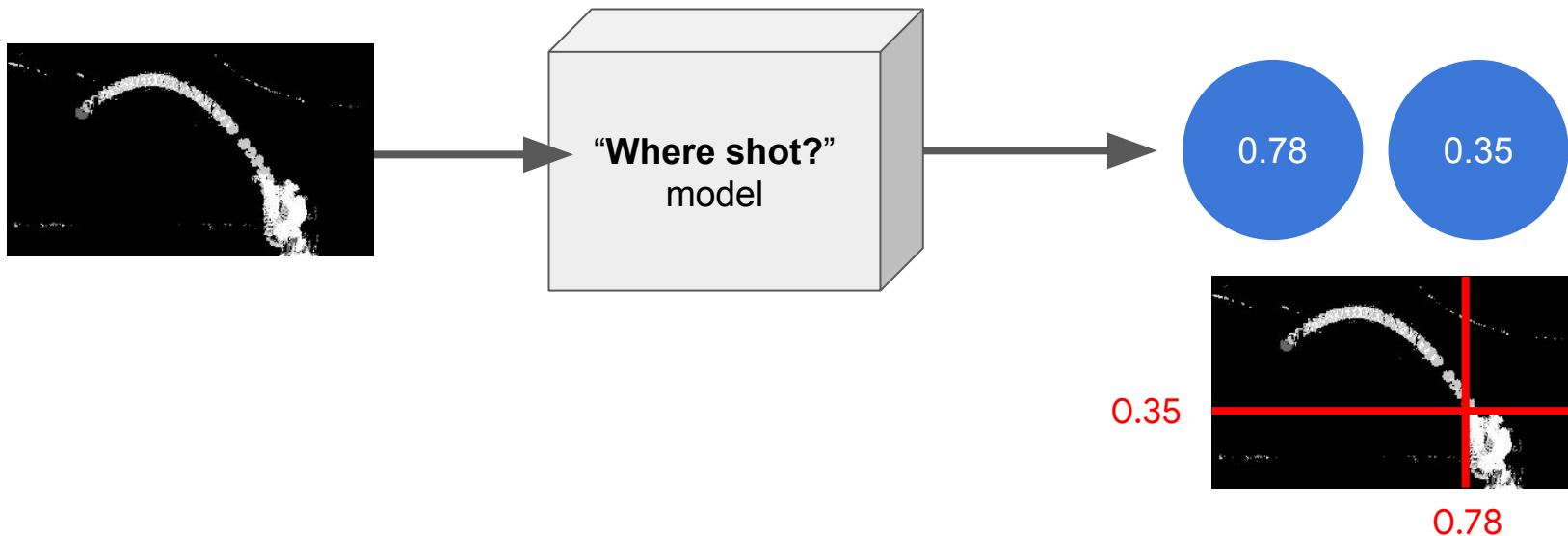
# Where to crop the image from?



Crop from (0.8, 0.3)

# Auto-cropping model

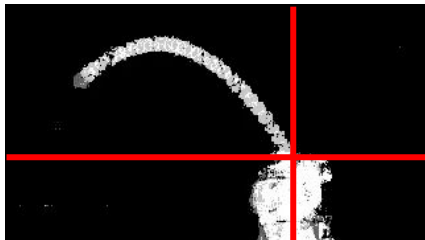
**Multi Target Regression Model**  
(predicting multiple numbers)



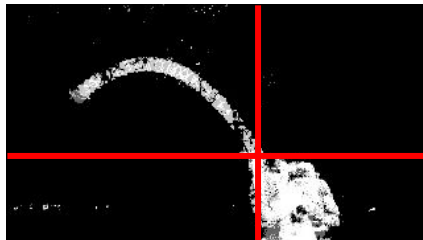


# Where to crop from?

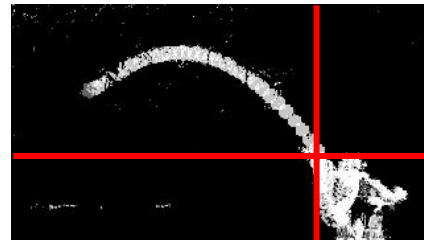
(0.8, 0.3)



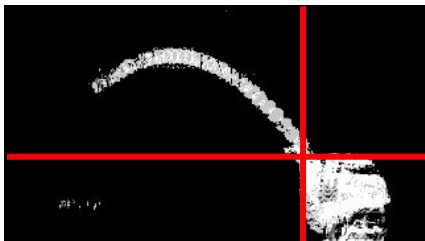
(0.76, 0.3)



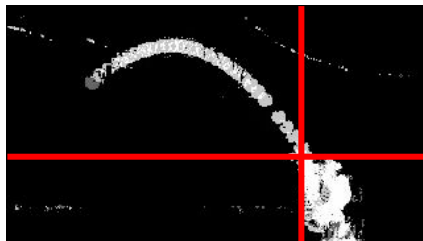
(0.66, 0.4)



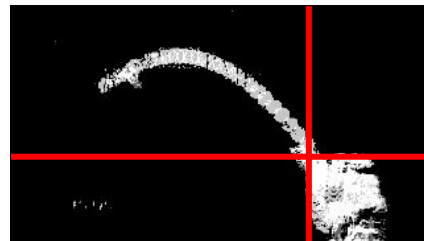
(0.7, 0.35)



(0.62, 0.41)



(0.76, 0.31)



# “Where shot?” model

**K** Keras

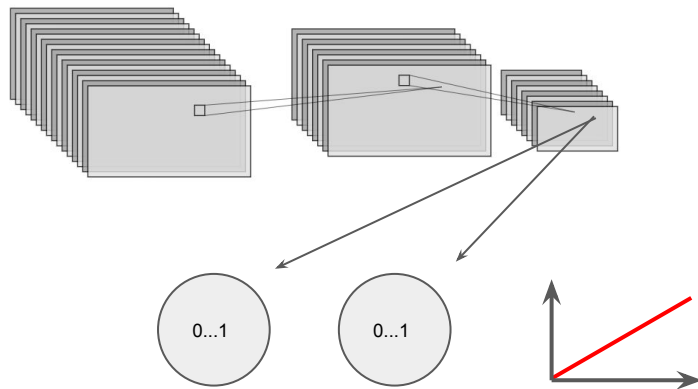
```
model = Sequential()

model.add(Conv2D(16, kernel_size=(3, 3),
                 activation='relu',
                 input_shape=input_shape))

model.add(Conv2D(8, (3, 3), activation='relu'))
model.add(MaxPooling2D(pool_size=(2, 2)))
model.add(Dropout(0.5))
model.add(Flatten())
model.add(Dense(16, activation='relu'))
model.add(Dropout(0.5))
model.add(Dense(2, activation='linear'))
```

## Convolutional Neural Network (CNN)

*(Good at image based tasks)*



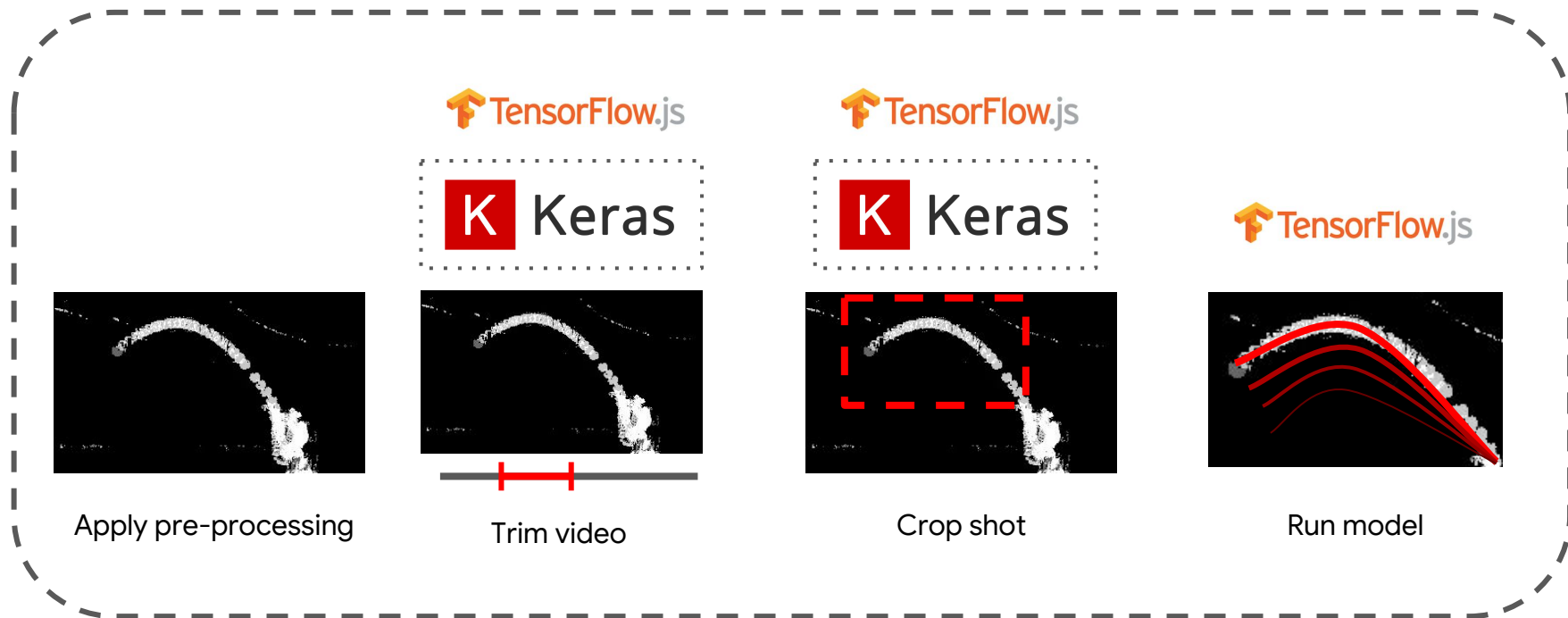


An outdoor basketball court with a black fence and asphalt floor. In the background, there are many trees with green and yellow leaves, suggesting autumn. A basketball hoop is visible on the left, and another one is on the right. A semi-transparent grey box is centered over the image.

**Shot Where demo**

**[bit.ly/zack-akil-hoops-where-demo](https://bit.ly/zack-akil-hoops-where-demo)**

# All together now!



Inside a webpage

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An outdoor basketball court with a black fence and asphalt surface. In the background, there are many trees with green and yellowing leaves, suggesting autumn. A basketball hoop is visible on the left, and another one is on the right. A semi-transparent grey rectangle is centered over the image, containing the text "Full demo".

**Full demo**

**[bit.ly/zack-akil-hoops-demo](https://bit.ly/zack-akil-hoops-demo)**



[bit.ly/zack-akil-hoops](https://bit.ly/zack-akil-hoops)

Gracias!



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